## **Example: Mealy Machine**<sub>JP</sub>

Define a Mealy machine that prints the one's complement of an input bit string. That is, the machine transforms every 0 to 1 and every 1 to 0. For example, the input string 0010 produces output 1101.

Recall that an Mealy machine is defined as a 5-tuple (Q,  $\Sigma$ ,  $\delta$ , q0, F) where

- Q is a finite set of states
- $\Sigma$  is a finite alphabet of symbols for forming the input string
- $\Gamma$  is the finite set of symbols in the output alphabet
- $\delta$  is the transition function,  $\delta: Q \times \Sigma \rightarrow Q \times \Gamma$
- q0 is the start state (q0 Q)

## **Sample Solution**

What are the input and output alphabets?

In this case, the input alphabet and output alphabet are identical:  $\Sigma = \Gamma = \{0, 1\}$ 

How is the transition function defined?

Consider that every transition must output the appropriate symbol for the input symbol just read. In this case, every  $\mathbf{0}$  in the input must result in an output of  $\mathbf{1}$ . Likewise, every  $\mathbf{1}$  in the input must result in an output of  $\mathbf{0}$ .

Note that when you define a transition for a Mealy machine in JFLAP, you must enter both the input symbol (left column) and the output symbol (right column).

Here is the sequence that demonstrates entering the two appropriate transitions:



Here is the resulting Mealy machine that prints the one's complement of an input bit string (see MEALY\_complement.jff):



Now step through input strings and observe the output. For example, the input string **0100101** produces output **1011010**.

|    | •      | •             |                   |      | J          | FLAP : | (MEALY_complement.jff) |   |
|----|--------|---------------|-------------------|------|------------|--------|------------------------|---|
| Fi | le     | Input         | Test              | View | Convert    | Help   |                        | × |
|    |        |               | Simulate: 1011010 |      |            |        |                        |   |
| Г  |        |               |                   |      |            |        |                        |   |
|    |        |               |                   |      |            |        |                        |   |
|    |        |               |                   |      |            |        | 1;0                    |   |
|    |        |               |                   |      |            |        | 0;1                    |   |
|    |        |               |                   |      |            |        |                        |   |
|    |        |               |                   |      |            |        |                        |   |
|    |        |               |                   |      |            |        |                        |   |
|    | ( q0 ) |               |                   |      |            |        |                        |   |
|    |        |               |                   |      |            | l      |                        |   |
|    |        |               |                   |      |            |        |                        |   |
|    |        |               |                   |      |            |        | ~                      |   |
|    | Xq     | <u>)</u> 101: | 1010              | {    |            |        |                        |   |
| [  | 010    | 0101          |                   |      |            |        |                        |   |
|    |        |               |                   |      |            |        |                        |   |
|    |        |               |                   |      |            |        |                        |   |
|    |        |               |                   |      |            |        |                        |   |
|    | Ste    | ep Reset      | Freeze            | Thaw | Trace Remo | ove    |                        |   |
|    |        |               |                   |      |            |        |                        |   |